

Assignment No 1

Max. Marks: 30

Subject and Subject code: Mathematics –I/ BTAM--101-23

Semester 1st (CSE/IT/AI-DS/AI-ML/IOT/DS/ECE/ME/RAI/E&CE)

Date on which assignment given: 13/08/2024 Date of submission of assignment: 28/08/2024

Course Outcomes:

Students will be able to:

CO1	Examine the convergence and divergence of sequences and series.
CO2	Apply the concept of Proper integral to find length , surface area and volume of revolution of the curves and to deal with discontinuous functions using Improper integral.
CO3	Use the concepts of partial differentiation to expand , estimate and find the extreme values of Multivariable Functions .
CO4	Evaluate area and volume of the surfaces using the concept of double and triple integration.

Bloom's Taxonomy Levels

L1 – Remembering, L2 – Understanding, L3 – Applying, L4 – Analysing, L5 – Evaluating, L6 - Creating

Assignment related to COs		Bloom's Taxonomy Level	Relevance to CO No.
SECTION - A (2Marks Each)			
Q1.	Explain the concept of Implicit and Explicit functions.	L-2	CO-3
Q2.	Define Oscillatory series with an example.	L-1	CO-1

Q3.	Show that the geometric series $\sum_{n=0}^{\infty} r^n$, where r is any real number such that $ r < 1$ is convergent.	L-3	CO-1
Q4.	What are the advantages and disadvantages of Lagrange's method of undetermined Multipliers?	L-2	CO-3
Q5.	Use the limit comparison test to determine whether the series $\sum (\sqrt[3]{n^3 - 1} - n)$ is convergent or divergent.	L-3	CO-1
SECTION – B (4 Marks Each)			
Q6.	Test the convergence of the series $\frac{x}{1.2} + \frac{x^2}{3.4} + \frac{x^3}{5.6} + \dots \infty$, where $x > 0$	L-4	CO-1
Q7.	If $u = \sin^{-1} \frac{x+y}{\sqrt{x}+\sqrt{y}}$, prove that $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + \frac{\partial^2 u}{\partial y^2} = -\frac{\sin u \cos 2u}{4 \cos^3 u}$	L-5	CO-3
Q8.	If $u=f(r)$ where $r^2 = x^2 + y^2$, show that $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f''(r) + \frac{1}{r} f'(r)$	L-4	CO-3
Q9.	A rectangular box open at the top, is to have volume of 32 cubic metres. Find the dimensions of the box requiring least material for its construction.	L-5	CO-3
Q10.	Test whether the series is conditionally convergent or not $\sum_{n=1}^{\infty} \frac{(-1)^{n-1} n}{n^2 + 1}$	L-6	CO-1